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## Formula Collection

## I. Return measures

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| discrete return | $\mathrm{R}_{\mathrm{t}}=\frac{P_{t}-P_{t-1}}{P_{t-1}}=\frac{P_{t}}{P_{t-1}}-1$ | $\begin{gathered} R_{t} \\ P_{t-1} \\ P_{t} \end{gathered}$ | $\begin{aligned} & =\text { return } \\ & =\text { price in period } \mathrm{t}-1 \\ & \text { (pervious period) } \\ & =\text { price in period } \mathrm{t} \end{aligned}$ |
| average return | $\bar{r}=\frac{r_{1}+r_{2}+\ldots+r_{T}}{T}=\frac{1}{T} \sum_{t=1}^{T} r_{t}$ | $\begin{gathered} \bar{r} \\ r_{t} \\ \mathrm{~T} \end{gathered}$ | ```= average return (expected return, mean return) \(=\) return in period t \(=\) number of periods``` |
| geometric return | $\bar{r}_{G}=\left[\left(1+r_{1}\right)\left(1+r_{2}\right) \ldots\left(1+r_{T}\right)\right]^{1 / T}-1$ | $\begin{gathered} r_{t} \\ \bar{r}_{G} \\ \mathrm{~T} \end{gathered}$ | $=$ return in period t $=$ geometric return $=$ number of periods |
| logarithmic return | $\ln \left(\frac{P_{t}}{P_{t-1}}\right)$ | $P_{t}$ | $=$ price in period t |
| multi period return (e.g. over 3 years) | $\left[\left(1+r_{1}\right)\left(1+r_{2}\right)\left(1+r_{3}\right)\right]-1$ | $r_{t}$ | $=$ return in period t |
| annual return | $R=\sqrt[T]{1+R}-1$ | T | = number of periods |
| return on equity | $\frac{\text { net income }}{E_{B}}=\frac{\text { EPS }}{E_{B} \text { per share }}$ | $\begin{gathered} E_{B} \\ \text { EPS } \end{gathered}$ | = Book value of equity <br> = Earnings per share |
| expected return | $E[r]=\mu=\sum_{i=1}^{n} p_{i} r_{i}$ | $\begin{gathered} \mu \\ \mathrm{n} \\ p_{i} \\ r_{i} \end{gathered}$ | = expected value <br> = number of scenarios <br> $=$ probability of scenario i <br> $=$ return for scenario i |
| stock return | $r=\frac{\left(P_{T}-P_{0}\right)+\operatorname{Div}_{t}}{P_{o}}=\frac{P_{T}-P_{0}}{P_{0}}+\frac{\operatorname{Div}_{t}}{P_{0}}$ | $P_{T}$ <br> $P_{0}$ <br> Div $_{t}$ | $=$ stock price at the end of the period <br> = stock price at the beginning $=$ dividend at the end of the period |

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## II. Statistical essentials - Portfolio management

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| expected value (average) | $\mathrm{E}(\mathrm{x})=\mu=\sum_{i=1}^{n} x_{\mathrm{i}} * p\left(x_{\mathrm{i}}\right)$ | $\begin{gathered} \mathrm{E}(\mathrm{x})= \\ \mu \\ x_{\mathrm{i}} \\ p\left(x_{\mathrm{i}}\right) \end{gathered}$ | = expected value <br> $=$ mean value <br> $=$ outcome $_{\mathrm{i}}$ <br> = probability of outcome $_{\mathrm{i}}$ |
| arithmetic mean | $\overline{\mathrm{x}}=\frac{1}{n} \sum_{i=1}^{n} x_{\mathrm{i}}$ | $\begin{gathered} \mathrm{n} \\ x_{i} \end{gathered}$ | $\begin{aligned} & =\text { number } \\ & =\text { outcome }_{\mathrm{i}} \end{aligned}$ |
| variance | $\operatorname{Var}(x)=\tilde{\sigma}^{2}=\sum_{i=1}^{n} p(x i) *\left(x_{i}-\overline{\mathrm{x}}\right)^{2}$ | $p\left(x_{\mathrm{i}}\right)$ | $=$ probability of outcome $_{\mathrm{i}}$ |
| sample variance | $\operatorname{Var}(x)=\tilde{\sigma}^{2}=\frac{1}{n-1} \sum_{t=1}^{n}\left(x_{i}-\overline{\mathrm{x}}\right)^{2}$ | $\begin{gathered} \mathrm{n} \\ x_{i} \\ \overline{\mathrm{x}} \end{gathered}$ | $\begin{aligned} & =\text { number } \\ & =\text { outcome }_{\mathrm{i}} \\ & =\text { arithmetic mean } \end{aligned}$ |
| standard deviation (volatility) | $\sigma=\sqrt{\operatorname{Var}(x)}=\sqrt{\sigma^{2}}$ | Var | = variance |
| volatility timescale | $\sigma=\tilde{\sigma} * \sqrt{t}$ | t | = time unit of sampling |
| semi variance | $\sigma^{2}=\frac{1}{n} \sum_{i=1}^{n}\left(\mathrm{x}_{\mathrm{i}}^{\text {negativ }}-\overline{\mathrm{x}}\right)^{2}$ | $\begin{gathered} \mathrm{n} \\ \mathrm{x}_{\mathrm{i}}^{\text {negativ }} \\ \overline{\mathrm{x}} \end{gathered}$ | $\begin{aligned} & =\text { number } \\ & =\text { negative outcome } \\ & =\text { arithmetic mean } \end{aligned}$ |
| covariance | $\operatorname{Cov}_{(1,2)}=\sum_{i=1}^{n} p_{i}\left[r_{i, 1}-E\left(r_{1}\right)\right]\left[r_{i, 2}-E\left(r_{2}\right)\right]$ | $\begin{gathered} \operatorname{Cov}_{1,2} \\ p_{i} \\ r_{i, 1} \\ r_{i, 2} \end{gathered}$ | = covariance between the return of asset 1 and 2 = probability of scenario i = return of asset 1 for scenario i $=$ return of asset 2 for scenario i |
| sample covariance | $\operatorname{Cov}_{1,2}=\frac{1}{n-1} \sum_{i=1}^{T}\left[r_{i, 1}-E\left(r_{1}\right)\right]\left[r_{i, 2}-E\left(r_{2}\right)\right]$ | $\begin{gathered} \operatorname{Cov}_{1,2} \\ \mathrm{~N} \end{gathered}$ | $\begin{aligned} & =\text { covariance between } \\ & \text { asset } 1 \text { and } 2 \\ & =\text { number of samples } \end{aligned}$ |

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| correlation coefficient | $p_{1,2}=\frac{\operatorname{Cov}_{1,2}}{\sigma_{1} \sigma_{2}}=\frac{\operatorname{Cov}_{1,2}}{\sqrt{\operatorname{Var}(R)_{1}} * \sqrt{\operatorname{Var}(R)_{2}}}$ | Cov <br> $\sigma_{1}$ <br> $\sigma_{2}$ | = covariance between the return of asset 1 and 2 = standard deviation (volatility) of asset 1 = standard deviation (volatility) of asset 2 |
| :---: | :---: | :---: | :---: |
| portfolio variance (2 Assets) | $\sigma_{p}^{2}=w_{1}^{2} \sigma_{1}^{2}+w_{2}^{2} \sigma_{2}^{2}+2 w_{1} w_{2} \operatorname{Cov}_{1,2}$ | w | = weight of asset i |
| portfolio variance <br> (3 Assets) | $\begin{aligned} \sigma^{2}= & w_{1}^{2} * \sigma_{1}^{2}+w_{2}^{2} * \sigma_{2}^{2}+w_{3}^{2} * \sigma_{3}^{2} \\ & +2 * w_{1} * w_{2} * \sigma_{1} * \sigma_{2} * p_{1,2} \\ & +2 * w_{2} * w_{3} * \sigma_{2} * \sigma_{3} * p_{2,3} \\ & +2 * w_{1} * w_{3} * \sigma_{1} * \sigma_{3} * p_{1,3} \end{aligned}$ |  |  |
| portfolio volatility | $\sigma_{P}=\sqrt{w_{1}^{2} \sigma_{1}^{2}+w_{2}^{2} \sigma_{2}^{2}+2 w_{1} w_{2} \operatorname{Cov}_{1,2}}$ <br> or $\sigma_{P}=\sqrt{w_{1}^{2} \sigma_{1}^{2}+w_{2}^{2} \sigma_{2}^{2}+2 w_{1} w_{2} p_{1,2} \sigma_{1} \sigma_{2}}$ | w <br> $\sigma$ <br> $p$ | $=$ weight of asset i <br> = standard deviation <br> (volatility) of Asset 1 <br> and 2 <br> = correlation <br> coefficient |
| portfolio volatility for a multi-assetportfolio | $\begin{aligned} \sigma_{\mathrm{p}}^{2}=\sum_{\mathrm{i}=1}^{\mathrm{n}} \mathrm{w}_{\mathrm{i}}^{2} * \sigma_{\mathrm{i}}^{2} & +2 \sum_{\mathrm{i}=1}^{n} \sum_{\mathrm{j}<1} \mathrm{p}_{\mathrm{ij}} * \mathrm{w}_{\mathrm{i}} * \mathrm{w}_{\mathrm{j}} * \sigma_{\mathrm{i}} * \sigma_{\mathrm{j}} \\ & \rightarrow \sqrt{\sigma_{\mathrm{p}}^{2}}=\sigma_{\mathrm{p}} \end{aligned}$ | $\mathrm{w}_{\mathrm{i}}$ <br> $\mathrm{w}_{\mathrm{j}}$ $\begin{gathered} \sigma_{i}^{2} \\ p_{i j} \end{gathered}$ | $\begin{aligned} & =\text { weight of }^{\text {asset }_{\mathrm{i}} \text { in } \%} \\ & =\text { weight of }^{\text {asset }_{j} \text { in } \%} \\ & =\text { variance of asset i } \\ & =\text { correlation } \\ & \text { coefficient } \end{aligned}$ |
| portfolio variance $\left(\sigma_{\mathrm{p}}^{2}\right)$ | $\begin{gathered} \sigma_{p}^{2}=\sum_{i=1}^{n} A_{i}^{2} * \sigma_{i}^{2} \\ +2 \sum_{i=1}^{n} \sum_{j<1} p_{i j} * A_{i} * A_{j} * \sigma_{i} * \sigma_{j} \end{gathered}$ | $\begin{gathered} A_{i} \\ \sigma_{i}^{2} \\ p_{i j} \\ \\ \mathrm{n} \\ \sigma_{i}, \sigma_{j} \end{gathered}$ | $\begin{aligned} & =\text { asset }_{\mathrm{i}} \\ & =\text { variance of asset } \mathrm{i} \\ & =\text { correlation } \\ & \text { coefficient between } \mathrm{i} \\ & \text { und } \mathrm{j} \\ & =\text { number of assets } \\ & =\text { standard deviation } \end{aligned}$ |
| $\mathrm{M}_{\text {Optimimum }}$ weight of asset A in a 2 -asset portfolio | $\begin{gathered} \frac{E\left(r_{A E}\right) * \sigma_{B}^{2}-E\left(r_{B E}\right) * \operatorname{Cov}\left(r_{A E}, r_{B E}\right)}{E\left(r_{A E}\right) * \sigma_{B}^{2}+E\left(r_{B E}\right) * \sigma_{A}^{2}-\left[E\left(r_{A E}\right)+E\left(r_{B E}\right)\right] * \operatorname{Cov}\left(r_{A E}, r_{B E}\right)} \\ \text { with: } \mathrm{r}_{\mathrm{AE}}=\mathrm{r}_{\mathrm{A}}-\mathrm{r}_{\mathrm{f}} \end{gathered}$ | $\sigma_{i}^{2}$ <br> Cov <br> $\mathrm{r}_{\mathrm{f}}$ | $=$ variance of asset i <br> = covariance between <br> the returns A, B <br> $=$ risk free return |


| minimum-varianceapproach | $\begin{gathered} x_{M V P}(A)=\frac{2 * \sigma_{B}^{2}-2 * \operatorname{Cov}\left(r_{A}, r_{B}\right)}{2 * \sigma_{A}^{2}+2 * \sigma_{B}^{2}-4 * \operatorname{Cov}\left(r_{A}, r_{B}\right)} \\ x_{M V P}(A)=\frac{\sigma_{B}^{2}-\operatorname{Cov}\left(r_{A}, r_{B}\right)}{\sigma_{A}^{2}+\sigma_{B}^{2}-2 * \operatorname{Cov}\left(r_{A}, r_{B}\right)} \\ x_{M V P}(A)=1-x_{M V P}(B) \end{gathered}$ | $\begin{gathered} \sigma_{i}^{2} \\ r_{A} \\ \\ \text { Cov } \end{gathered}$ | $=$ variance of asset i <br> $=$ return of the asset <br> A <br> = covariance between <br> the returns of asset A <br> and B |
| :---: | :---: | :---: | :---: |
| portfolio-beta | $\beta_{\text {Portfolio }}=\sum_{i=1}^{N} x_{p, i} * \beta_{i}$ | $\begin{gathered} \mathrm{X}_{\mathrm{P}, \mathrm{i}} \\ \beta_{i} \end{gathered}$ | $=$ weight of asset i in the portfolio = beta of asset i |
| excess return | $r_{a}=r_{P}-r_{B}$ | $\begin{aligned} & r_{p} \\ & r_{B} \end{aligned}$ | $\begin{aligned} & =\text { return Portfolio } \\ & =\text { return Benchmark } \end{aligned}$ |
| market-timing | $r_{\text {timing }}=\sum_{i=1}^{N}\left(x_{p, i}-x_{B, i}\right) * r_{B, i}$ | $X_{P, i}$ <br> $\mathrm{X}_{\mathrm{B}, \mathrm{i}}$ <br> $r_{B, i}$ | $=$ weight of asset i in the portfolio = weight of asset i in the benchmark $=$ return i in the benchmark |
| selection effect | $r_{\text {selection }}=\sum_{i=1}^{N}\left(r_{p, i}-r_{B, i}\right) * x_{B, i}$ | $\mathrm{r}_{\mathrm{P}, \mathrm{i}}$ | $=$ return i in the portfolio |
| interaction effect | $r_{\text {Interaction }}=\sum_{i=1}^{N}\left(x_{p, i}-x_{B, i}\right) *\left(r_{p, i}-r_{B, i}\right)$ |  |  |

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## III. Cost of Capital

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| WACC | $r_{E} * \frac{E}{E+D}+r_{D} * \frac{D}{E+D}$ | $\begin{gathered} \mathrm{r}_{\mathrm{E}} \\ \mathrm{r}_{\mathrm{D}} \\ \mathrm{E} \\ \mathrm{D} \end{gathered}$ | $\begin{aligned} & =\text { return on equity } \\ & =\text { return on debt } \\ & =\text { equity } \\ & =\text { debt } \end{aligned}$ |
| WACC after taxes | $\mathrm{r}_{\mathrm{E}} * \frac{\mathrm{E}}{\mathrm{E}+\mathrm{D}}+\mathrm{r}_{\mathrm{D}} * \frac{\mathrm{D}}{\mathrm{E}+\mathrm{D}} *\left(1-t_{m}\right)$ | $\begin{gathered} \mathrm{E} \\ \mathrm{D} \\ t_{m} \end{gathered}$ | $\begin{aligned} & =\text { equity } \\ & =\text { debt } \\ & =\text { marginal tax rate } \end{aligned}$ |
| return on equity <br> ( $\mathrm{M} \& \mathrm{M}$ ) | $\mathrm{WACC}+\left(\mathrm{WACC}-\mathrm{r}_{\mathrm{D}}\right) * \frac{\mathrm{D}}{\mathrm{E}}$ | $\begin{gathered} \text { WACC } \\ \\ \mathrm{r}_{\mathrm{D}} \\ \mathrm{D} \\ \mathrm{E} \end{gathered}$ | $=$ Weighted <br> Average Cost of <br> Capital <br> = return on debt <br> $=$ debt <br> = equity |
| expected return (CAPM) | $E\left(r_{k}\right)=i_{\text {riskfree }}+\beta *\left(E\left(r_{M}\right)-i_{\text {riskfree }}\right)+\varepsilon_{k}$ | $i_{\text {riskfree }}$ $\begin{gathered} \beta \\ E\left(r_{M}\right) \\ \varepsilon_{k} \end{gathered}$ | $=$ risk free rate <br> = beta factor <br> = expected return of the market portfolio $=$ specific risk |
| expected return 3-factormodel Fama/French | $\begin{array}{r} E\left(r_{k}\right)=i_{\text {riskfree }}+\beta_{M} *\left(E\left(r_{M}\right)-i_{\text {riskfree }}\right)+\beta_{S} \\ * E(S M B)+\beta_{H} * E(H M L)+\varepsilon_{k} \end{array}$ | $\begin{gathered} \beta_{S} \\ E(S M B) \\ \beta_{H} \\ E(H M L) \end{gathered}$ | $=$ Beta small minus big -effect = factor small minus big-effect = Beta high minus low-effect $=$ factor high minus low-effect |
| beta-factor CAPM | $\beta_{k}=\frac{\sigma_{k} * p_{k, M}}{\sigma_{M}}=\frac{\operatorname{Cov}_{(\mathrm{k}, \mathrm{M})}}{\sigma_{\mathrm{M}}^{2}}$ | $\begin{gathered} \sigma_{k} \\ p_{k, M} \\ \\ \sigma_{M} \\ \operatorname{Cov}_{(\mathrm{k}, \mathrm{M})} \\ \sigma_{M}^{2} \end{gathered}$ | $=$ standard deviation of asset k = correlation between asset k and the market portfolio = standard deviation market portfolio $=$ covariance $_{(\mathrm{k}, \mathrm{M})}$ = variance market portfolio |

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|  | $r_{E}=\frac{D i v_{1}+P_{1}}{P_{0}}-1=\frac{D i v_{1}}{P_{0}}+\frac{P_{1}-P_{0}}{P_{0}}$ | $\mathrm{P}_{0}$ <br> $\mathrm{P}_{1}$ | stock price today <br> stock price in one <br> cost of equity (DDM- <br> Model) |
| :---: | :---: | :---: | :--- |
| or $\frac{D i v_{1}}{P_{0}}+g$ | Div $_{1}$ | year <br> dividend in one <br> year <br> growth rate |  |

## IV. Corporate analysis

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| debt ratio | $\frac{D}{D+E}$ | $\begin{aligned} & \mathrm{D} \\ & \mathrm{E} \end{aligned}$ | $\begin{aligned} & =\text { debt } \\ & \text { = Equity } \end{aligned}$ |
| equity ratio | $\frac{E}{D+E}$ | $\begin{aligned} & \mathrm{D} \\ & \mathrm{E} \end{aligned}$ | $\begin{aligned} & =\text { debt } \\ & \text { = Equity } \end{aligned}$ |
| debt to equity ratio | $\frac{D}{E}$ | $\begin{aligned} & \mathrm{D} \\ & \mathrm{E} \end{aligned}$ | $\begin{aligned} & =\text { debt } \\ & \text { = Equity } \end{aligned}$ |
| dynamic leverage ratio | liabilities - Cash \& Short Term Investments Cash Flow from Operating Activities |  |  |
| interest coverage ratio | $\frac{E B I T}{\text { interest expenses }}$ |  |  |
| capital repayment ratio | $\frac{E B I T D A}{D+E}$ |  |  |
| ROCE | $\frac{E B I T}{D+E}$ |  |  |
| quick ratio | $\frac{\text { Cash }+C E+M S+A R}{\text { current liabilities }}$ | CE <br> MS <br> AR | = Cash equivalents <br> = marketable <br> securities <br> = accounts <br> receivable |
| liabilities repayment ratio | $\frac{\text { Free Cashflow }}{D}$ |  |  |
| gross margin | $\frac{\text { Gross profit on sales }}{\text { revenue }}$ |  |  |
| EBIT-margin | $\frac{\text { EBIT }}{\text { revenue }}$ |  |  |

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| return on sales | $\frac{\text { net income }}{\text { revenue }}$ |  |  |
| :---: | :---: | :---: | :---: |
| return on assets | net income + interest expenditures total capital |  |  |
| return on investment | $\frac{\text { net income }}{\text { revenue }} * \frac{\text { revenue }}{\text { total capital }}$ |  |  |
| par value per share | $\frac{\text { share capital }}{N(S)}$ | N(S) | $=$ number of shares |
| number of shares | $\frac{\text { share capital }}{\text { par value of a share }}$ |  |  |
| earnings per share | $\begin{gathered} \frac{\text { earnings after taxes }}{\mathrm{N}(\mathrm{~S})} \\ = \\ \text { book value per share } * \text { return on equity } \end{gathered}$ |  |  |
| dividend per share | $\frac{\text { earnings after taxes } * \text { payout ratio }}{\mathrm{N}(\mathrm{~S})}$ |  |  |
| new share price after raising new capital | $\mathrm{M}=\frac{K_{a} * n_{a}+K_{n} * n_{n}}{n_{a}+n_{n}}$ | $\begin{aligned} & K_{a} \\ & n_{a} \\ & K_{n} \\ & n_{n} \end{aligned}$ | ```= old shares price = number of old shares = new shares price = number of new shares``` |
| subscription ratio | $\text { SRatio }=\frac{n_{a}}{n_{n}}$ |  |  |
| subscription rights | $\begin{aligned} & \text { SRights }=K_{a}-M \\ & \text { SRights }=\frac{K_{a}-K_{n}}{\frac{n_{a}}{n_{n}}+1} \end{aligned}$ |  |  |
| operation blanche | $\frac{\text { number of SRights } * \text { price SRights }}{\text { New share price after a capital raise }}$ | SRights | = subscription rights |
| dividend yield | $\frac{\text { dividend per share }}{\text { price per share }} * 100$ |  |  |
| dividend per share | $\frac{\text { net } \text { income }_{t}}{N(S)} * \text { payout ratio }$ | N(S) | = outstanding shares |

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| retention ratio | $1-\frac{\text { Div }}{\text { EPS }}$ | $\begin{aligned} & \text { Div } \\ & \text { EPS } \end{aligned}$ | $\begin{aligned} & =\text { dividend } \\ & \text { = earnings per share } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| growth rate | $g=\frac{\text { change in profit }}{\text { profit }}$ <br> or $g=\text { retention ratio } * \text { ROE }$ |  |  |
| earnings value | $\frac{\text { average income per year }}{i}$ | i | = discount rate |
| book value per share | $\frac{(\text { book value) equity }}{N(S)}$ | $\mathrm{N}(\mathrm{S})$ | = number of shares |
| price to book ratio | $\frac{\text { share price }}{\text { book value per share }}=\frac{\text { market capitalisation }}{\text { equity }}$ |  |  |
| price earnings ratio | $\begin{gathered} \frac{P_{0}}{E P S_{1}}=\frac{1}{c-g} \\ E P S_{1}=E P S_{0} *(1+g) \end{gathered}$ | $\begin{gathered} P_{0} \\ E P S_{1} \\ \mathrm{~g} \\ \mathrm{c} \end{gathered}$ | = price of the asset <br> = expected earnings <br> per share in one <br> year <br> = growth rate <br> $=$ cost of capital |
| price to cashflow ratio | $\frac{P_{0}}{\text { Cashflow per share }}$ | $P_{0}$ | = share price |
| PEG | $\frac{K G V}{\text { profit growth }}$ | PEG | $=$ Price-Earnings- <br> to-Growth-Ratio |

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## V. Corporate valuation

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| market capitalization | $P_{0} * N(S)$ | $\begin{gathered} \mathrm{N}(\mathrm{~S}) \\ P_{0} \end{gathered}$ | $\begin{aligned} & =\text { number of shares } \\ & =\text { share price today } \end{aligned}$ |
| share price <br> (Dividend-DiscountModel) | $P_{0}=\frac{D i v_{1}+P_{1}}{1+r_{E}}$ | $P_{0}$ <br> $D i v_{1}$ <br> $P_{1}$ <br> $r_{E}$ | $=$ Price of the asset <br> in t 0 <br> $=$ dividend in tl <br> $=$ Price of the asset <br> in t 1 <br> = expected return |
| share price (DDM-multi periods) | $P_{0}=\frac{\operatorname{Div}_{1}}{1+r_{E}}+\frac{\operatorname{Div}_{2}}{\left(1+r_{E}\right)^{2}}+\cdots \frac{\operatorname{Div}_{n}+P_{n}}{\left(1+r_{E}\right)^{\wedge} \mathrm{n}}$ |  |  |
| share price (DDM constant growth) | $P_{0}=\frac{D i v_{1}}{r_{E}-g}$ | g | $=$ growth rate |
| enterprise value | market value equity + debt - cash |  |  |
| enterprise value <br> (DCF-Modell) | $\begin{aligned} = & \sum_{t=1}^{T} \frac{F C F_{t}}{(1+i)^{t}}+\frac{T V_{T}}{(1+i)^{T}} \\ & \text { with } \mathrm{TV}_{\mathrm{T}}=\frac{C F t+1}{i-g} \end{aligned}$ | $\begin{gathered} \mathrm{FCF}_{\mathrm{t}} \\ \mathrm{TV}_{\mathrm{T}} \\ \mathrm{i} \\ \mathrm{~g} \end{gathered}$ | $\begin{aligned} & =\text { free-cashflow in } \\ & \text { period } \mathrm{t} \\ & =\text { terminal value } \\ & =\text { discount rate } \\ & =\text { growth rate } \end{aligned}$ |
| share price in $\mathrm{t}_{0}$ | $\mathrm{P}_{0}=\frac{\mathrm{PV}(\text { future total dividends }+ \text { repurchases })}{N(S)}$ | $\begin{gathered} \text { PV } \\ \mathrm{N}(\mathrm{~S}) \end{gathered}$ | = present value <br> = outstanding <br> shares |
| enterprise value (perpetuity) | $\frac{\mathrm{FCF}}{i}$ | $\begin{gathered} \text { FCF } \\ \text { i } \end{gathered}$ | $\begin{aligned} & =\text { free cashflow } \\ & =\text { discount rate } \end{aligned}$ |
| share price in $\mathrm{t}_{0}$ | $\frac{\mathrm{V}_{0}+\mathrm{Cash}_{0}-\mathrm{Debt}_{0}}{\mathrm{~N}(\mathrm{~S})}$ | $\begin{gathered} V_{0} \\ \mathrm{~N}(\mathrm{~S}) \end{gathered}$ | $\begin{aligned} & =\text { enterprise value } \\ & =\text { outstanding } \\ & \text { shares } \end{aligned}$ |
| tax shield | corporate tax rate * interest payment |  |  |
| enterprise value $\left(V_{l}\right)$ | $V_{u}+P V($ Tax Shield $)-P V($ Financial distress $)$ | $\begin{aligned} & V_{l} \\ & V_{u} \end{aligned}$ | = enterprise value levered firm =enterprise value unlevered firm |
| EV/ EBITDA multiple | $\frac{\mathrm{V}_{0}}{E B I T D A}$ |  |  |

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| equity multiple <br> (book value) | $\frac{\text { Total Assets }}{E_{B}}$ | $E_{B}$ | $=$ Book Value <br> equity |
| :---: | :---: | :---: | :--- |
| equity multiple <br> (market value) | $\frac{\text { Total Assets }}{E_{M}}$ | $E_{M}$ | $=$ Market Value <br> equity |
| value additivity | $\mathrm{P}(\mathrm{C})=\mathrm{P}(\mathrm{A}+\mathrm{B})=\mathrm{P}(\mathrm{A})+\mathrm{P}(\mathrm{B})$ | P | $=$ Price |

## VI. Risk indicators and Risk Management

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| Sharpe-Ratio | $\frac{\left(\hat{r}_{\text {Portfolio }}-i_{\text {riskfree }}\right)}{\sigma_{\text {Portfolio }}}$ | $\hat{r}_{\text {Portfolio }}$ <br> $i_{\text {riskfree }}$ <br> $\sigma_{\text {Portfolio }}$ | $\begin{aligned} & \text { = average return } \\ & \text { portfolio } \\ & \text { = risk-free rate } \\ & \text { = portfolio volatility } \end{aligned}$ |
| SCML (Growth capital market line) | $\frac{r_{M}-i_{\text {riskfree }}}{\sigma_{M}}$ | $i_{\text {riskfree }}$ <br> $r_{M}$ <br> $\sigma_{M}$ | = risk-free rate <br> = return market <br> portfolio <br> = volatility market portfolio |
| Treynor-Ratio | $\frac{\hat{r}_{\text {Portfolio }}-i_{\text {riskfree }}}{\beta_{\text {Portfolio }}}$ | $\hat{r}_{\text {Portfolio }}$ <br> $i_{\text {riskfree }}$ <br> $\beta_{\text {Portfolio }}$ | $\begin{aligned} & \text { = average return } \\ & \text { portfolio } \\ & =\text { risk-free rate } \\ & =\text { beta factor } \\ & \text { portfolio } \end{aligned}$ |
| Jensen-Alpha | $\begin{gathered} \left(\hat{r}_{\text {Portfolio }}-i_{\text {riskfree }}\right)-\left(\hat{r}_{\text {Benchmark }}-i_{\text {riskfree }}\right) \\ * \beta_{\text {Portfolio }}+\varepsilon \end{gathered}$ | $\hat{r}_{\text {Benchmark }}$ | = average return <br> benchmark |
| Value at Risk (VaR) | $\mathrm{VaR}=\mathrm{RP} * \sigma * \mathrm{~N}(\mathrm{x}) * \sqrt{t}$ | $\begin{gathered} \mathrm{RP} \\ \sigma \\ \mathrm{~N}(\mathrm{x}) \\ \sqrt{t} \end{gathered}$ | $\begin{aligned} & \text { = risk position } \\ & \text { = volatility } \\ & =\text { confidence level } \\ & =\text { liquidation period } \end{aligned}$ |
| marginal Value at Risk $\left(\Delta V a R_{i}\right)$ | $=\mathrm{N}(\mathrm{x}) * \frac{\operatorname{cov}_{(\mathrm{x}, \mathrm{y})}}{\sigma_{\text {portfolio }}}$ | $\begin{aligned} & \operatorname{COV}_{(\mathrm{x}, \mathrm{y})} \\ & N(\mathrm{x}) \end{aligned}$ | $\begin{aligned} & =\text { covariance } \\ & =\text { confidence level } \end{aligned}$ |
| incremental Value at Risk | $\operatorname{VaR}_{\mathrm{i}}=\mathrm{N}_{\mathrm{i}} * \beta_{\mathrm{i}} * \sigma_{\mathrm{p}} * \mathrm{a}_{\mathrm{i}}$ | $\begin{aligned} & N_{i} \\ & \mathrm{~B}_{\mathrm{i}} \\ & \mathrm{a}_{\mathrm{i}} \end{aligned}$ | = confidence level <br> = beta factor <br> = amount of the <br> increased asset |

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| component Value at Risk | $\mathrm{CoVaR}_{\mathrm{i}}=$ Portfolio VaR $* \bigcap_{i} * \mathrm{w}_{\mathrm{i}}$ | $\begin{gathered} \beta_{i} \\ w_{i} \end{gathered}$ | $\begin{aligned} & =\text { beta factor } \\ & =\text { weight of asset i } \\ & \text { in } \% \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| Value at Risk adjustment of liquidation period | $\mathrm{VaR}_{\mathrm{t}}=\mathrm{VaR} * \sqrt{\mathrm{t}}$ | $\begin{gathered} \mathrm{VaR} \\ \mathrm{t} \end{gathered}$ | $\begin{aligned} & =\text { value at Risk } \\ & =\text { time period } \end{aligned}$ |
| Value at Risk adjustment of confidence level | $\operatorname{VaR}\left(\mathrm{x}^{*}\right)=\operatorname{VaR}(\mathrm{x}) * \frac{\mathrm{~N}\left(\mathrm{x}^{*}\right)}{\mathrm{N}(\mathrm{x})}$ | $\begin{aligned} & \mathrm{N}\left(\mathrm{x}^{*}\right) \\ & \mathrm{N}(\mathrm{x}) \end{aligned}$ | $\begin{aligned} & \text { = new confidence } \\ & \text { level } \\ & \text { = confidence level } \end{aligned}$ |
| cost of capital with risk premium | $=\frac{M R P}{\operatorname{VaR}\left(r_{M}\right)}=\frac{r_{M}-i_{\text {riskfree }}}{-\left(r_{M}+N(x) * \sigma_{M}\right)}$ | MRP | $=$ market risk premium |
| cost of capital based on earnings risk | $\frac{1+i_{\text {riskfree }}}{1-\lambda * V * d}-1$ | $\lambda$ <br> V <br> d | ```= excess return per unit of risk (shape ratio) = coefficient of variation of the returns =risk diversification factor``` |
| insurance premium | $\frac{[\operatorname{Pr}(\text { loss }) * E(\text { Payment in the loss event })]}{1+c}$ | c | = cost of capital |
| default risk | PD * amount of risk default | PD | $=$ probability of default |
| return on risk-adjusted capital (RoRaC) | $\begin{gathered} =\frac{\text { net income }}{\text { allocated risk capital }} \\ =\frac{\text { price gain }- \text { risk free interest rate }}{\text { CoVaR }} \\ =\frac{\text { revenue }- \text { costs }}{\text { CoVaR }} \end{gathered}$ | CoVaR | $=$ Component Value at risk |
| risk-adjusted return on capital (RaRoC) | $\begin{aligned} & =\frac{\text { risk adjusted net income }}{(\text { economic risk) capital }} \\ & =\frac{\text { Net income }- \text { risk capital }}{(\text { economic risk) capital }} \end{aligned}$ |  |  |


| expected loss | PD * LGD * EaD | $\begin{gathered} \text { PD } \\ \text { LGD } \\ \text { EaD } \end{gathered}$ | $=$ probability of default <br> $=$ loss given default <br> / recovery rate <br> = exposure at <br> default / credit <br> default |
| :---: | :---: | :---: | :---: |
| risk-adjusted lending <br> rates <br> $\rightarrow$ equity capital costs | 1. standard deviation of loss rate in $\%$ <br> 2. $\sigma_{\mathrm{PD}}=\sqrt{\mathrm{PD} *(1-\mathrm{PD})}$ <br> 3. credit $\operatorname{VaR}(\mathrm{CVaR})=$ $\mathrm{EaD} * \sqrt{\mathrm{PD} * \sigma_{\mathrm{LGD}}^{2}+\mathrm{LGD}^{2} * \sigma_{\mathrm{PD}}^{2}}$ <br> 4. Equity costs ${ }_{€}=\mathrm{CVaR} *$ Equity costs $\%$ | $\sigma_{\text {LGD }}$ <br> $\sigma_{\mathrm{PD}}$ <br> $\sigma_{\text {LGD }}^{2}$ <br> $\sigma_{P D}^{2}$ <br> CVaR | = volatility of the loss given default = volatility of the probability of default <br> = variance of the loss given default = variance of the loss given default = Credit Value at risk |
| CVaR of a credit portfolio | $\sqrt{\mathrm{CVaR}_{\mathrm{A}}^{2}+\mathrm{CVaR}_{\mathrm{B}}^{2}+2 * \mathrm{CVaR}_{\mathrm{A}} * \mathrm{CVaR}_{\mathrm{B}} * p_{1,2}}$ | $p_{A, B}$ | = correlation coefficient of A and B |
| portfolio-hedge | $\text { Hedge-Ratio }=\frac{\text { portfolio value }}{\text { (Index } * \text { contract value) }} * \text { Beta }$ |  |  |

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## VII. Working Capital Management

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| working capital | Current assets - current liabilities |  |  |
| cost of holding working capital | working capital * c | c | $=$ cost of capital |
| cash conversion cycle | $\emptyset$ days in inventory $+\emptyset$ collection period $-\emptyset$ payment period | $\emptyset$ | $=$ average |
| inventory days outstanding (DIO) | $\frac{\emptyset \text { inventory }}{\text { cost of goods sold }} * 365$ |  |  |
| days sales outstanding (DSO) | $\frac{\varnothing \text { accounts receivable }}{\text { sales }} * 365$ |  |  |
| days payable outstanding (DPO) | $\frac{\emptyset \text { accounts payable }}{\text { cost of goods sold }} * 365$ |  |  |

## VIII. Bond valuation



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| coupon payment <br> (coupon bonds) | $\frac{\text { Coupon Rate } * \mathrm{FV}}{\text { Number Payments per Year }}$ | FV | $=$ face value |
| :---: | :---: | :---: | :--- |
| yield to Maturity | $\left(\frac{\mathrm{FV}}{\mathrm{P}}\right)^{\frac{1}{t}}-1$ | $t$ <br> P | = period <br> Price |
| price bond | $\mathrm{CPN} * \frac{1}{\mathrm{Y}}\left(1-\frac{1}{(1+\mathrm{Y})^{t}}\right)+\frac{\mathrm{FV}}{(1+\mathrm{Y})^{t}}$ | CPN | Y Coupon Payment <br> = Yield to maturity |

## IX. Derivatives

| Name | Formula | Explanation |  |
| :---: | :---: | :---: | :---: |
| option price | Intrinsic value + time value |  |  |
| intrinsic value call option | $P_{0}-$ strike price | $P_{0}$ | = Current Market <br> Price of Underlying <br> Asset |
| intrinsic value put option | strike price $-P_{0}$ | $P_{0}$ | = Current Market <br> Price of Underlying <br> Asset |
| time value option | Option price - positive intrinsic value |  |  |
| leverage option | $\frac{P_{0}}{(\text { Option price } * S R)}$ | $\begin{gathered} P_{0} \\ \mathrm{SR} \end{gathered}$ | $\begin{aligned} & =\text { share price } \\ & =\text { subscription ratio } \end{aligned}$ |
| future Price | $\begin{gathered} \mathrm{F}_{0}=\mathrm{S}_{0} \mathrm{e}^{(\mathrm{r}-\mathrm{q}) * \mathrm{~T}} \\ \mathrm{~F}_{0}=\mathrm{S}_{0} \mathrm{e}^{(\mathrm{r}-\mathrm{rf}) * \mathrm{~T}} \\ \mathrm{~F}_{0}=\left(\mathrm{S}_{0}+\mathrm{U}_{\mathrm{PV}}\right) \mathrm{e}^{\mathrm{rT}} \end{gathered}$ | e <br> $\mathrm{S}_{0}$ <br> T <br> $r$ <br> q <br> $\mathrm{r}_{\mathrm{f}}$ <br> $\mathrm{U}_{\mathrm{PV}}$ | ```= number of Euler = Price underlying asset today = time to maturity = risk-free rate = dividend yield = foreign risk-free rate = present value storage costs``` |

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## X. Other Calculations

| net present value | $N P V=-C+\sum_{t=1}^{n} \frac{C F_{t}}{(1+i)^{t}}$ | $C F_{t}$ <br> i <br> t <br> C | $\begin{aligned} & =\text { cashflow in } \\ & \text { period } \mathrm{t} \\ & \text { = discount rate } \\ & =\text { period of the } \\ & \text { cashflow } \\ & \text { = initial investment } \end{aligned}$ |
| :---: | :---: | :---: | :---: |
| net present value with probability of bankruptcy | $N P V=-C+\sum_{t=1}^{n} \frac{C F_{t} *\left(1-P_{B}\right)^{t}}{(1+i)^{t}}$ | $P_{B}$ | $=$ probability of bankruptcy |
| present value with probability of bankruptcy (perpetuity) | $P V=\frac{C F *\left(1-P_{B}\right)}{i+P_{B}}$ | $P_{B}$ | $=$ probability of bankruptcy |

## Required statistic table: Normal distribution

| $z$ | . 00 | . 01 | . 02 | . 03 | . 04 | . 05 | . 06 | . 07 | . 08 | . 09 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0 | . 5000 | . 5040 | . 5080 | . 5120 | . 5160 | . 5199 | . 5239 | . 5279 | . 5319 | . 5359 |
| 0.1 | . 5398 | . 5438 | . 5478 | . 5517 | . 5557 | . 5596 | . 5636 | . 5675 | . 5714 | . 5753 |
| 0.2 | . 5793 | . 5832 | . 5871 | . 5910 | . 5948 | . 5987 | . 6026 | . 6064 | . 6103 | . 6141 |
| 0.3 | . 6179 | . 6217 | . 6255 | . 6293 | . 6331 | . 6368 | . 6406 | . 6443 | . 6480 | . 6517 |
| 0.4 | . 6554 | . 6591 | . 6628 | . 6664 | . 6700 | . 6736 | . 6772 | . 6808 | . 6844 | . 6879 |
| 0.5 | . 6915 | . 6950 | . 6985 | . 7019 | . 7054 | . 7088 | . 7123 | . 7157 | . 7190 | . 7224 |
| 0.6 | . 7257 | . 7291 | . 7324 | . 7357 | . 7389 | . 7422 | . 7454 | . 7486 | . 7517 | . 7549 |
| 0.7 | . 7580 | . 7611 | . 7642 | . 7673 | . 7704 | . 7734 | . 7764 | . 7794 | . 7823 | . 7852 |
| 0.8 | . 7881 | . 7910 | . 7939 | . 7967 | . 7995 | . 8023 | . 8051 | . 8078 | . 8106 | . 8133 |
| 0.9 | . 8159 | . 8186 | . 8212 | . 8238 | . 8264 | . 8289 | . 8315 | . 8340 | . 8365 | . 8389 |
| 1.0 | . 8413 | . 8438 | . 8461 | . 8485 | . 8508 | . 8531 | . 8554 | . 8577 | . 8599 | . 8621 |
| 1.1 | . 8643 | . 8665 | . 8686 | . 8708 | . 8729 | . 8749 | . 8770 | . 8790 | . 8810 | . 8830 |
| 1.2 | . 8849 | . 8869 | . 8888 | . 8907 | . 8925 | . 8944 | . 8962 | . 8980 | . 8997 | . 9015 |
| 1.3 | . 9032 | . 9049 | . 9066 | . 9082 | . 9099 | . 9115 | . 9131 | . 9147 | . 9162 | . 9177 |
| 1.4 | . 9192 | . 9207 | . 9222 | . 9236 | . 9251 | . 9265 | . 9279 | . 9292 | . 9306 | . 9319 |
| 1.5 | . 9332 | . 9345 | . 9357 | . 9370 | . 9382 | . 9394 | . 9406 | . 9418 | . 9429 | . 9441 |
| 1.6 | . 9452 | . 9463 | . 9474 | . 9484 | . 9495 | . 9505 | . 9515 | . 9525 | . 9535 | . 9545 |
| 1.7 | . 9554 | . 9564 | . 9573 | . 9582 | . 9591 | . 9599 | . 9608 | . 9616 | . 9625 | . 9633 |
| 1.8 | . 9641 | . 9649 | . 9656 | . 9664 | . 9671 | . 9678 | . 9686 | . 9693 | . 9699 | . 9706 |
| 1.9 | . 9713 | . 9719 | . 9726 | . 9732 | . 9738 | . 9744 | . 9750 | . 9756 | . 9761 | . 9767 |
| 2.0 | . 9772 | . 9778 | . 9783 | . 9788 | . 9793 | . 9798 | . 9803 | . 9808 | . 9812 | . 9817 |
| 2.1 | . 9821 | . 9826 | . 9830 | . 9834 | . 9838 | . 9842 | . 9846 | . 9850 | . 9854 | . 9857 |
| 2.2 | . 9861 | . 9864 | . 9868 | . 9871 | . 9875 | . 9878 | . 9881 | . 9884 | . 9887 | . 9890 |
| 2.3 | . 9893 | . 9896 | . 9898 | . 9901 | . 9904 | . 9906 | . 9909 | . 9911 | . 9913 | . 9916 |
| 2.4 | . 9918 | . 9920 | . 9922 | . 9925 | . 9927 | . 9929 | . 9931 | . 9932 | . 9934 | . 9936 |
| 2.5 | . 9938 | . 9940 | . 9941 | . 9943 | . 9945 | . 9946 | . 9948 | . 9949 | . 9951 | . 9952 |
| 2.6 | . 9953 | . 9955 | . 9956 | . 9957 | . 9959 | . 9960 | . 9961 | . 9962 | . 9963 | . 9964 |
| 2.7 | . 9965 | . 9966 | . 9967 | . 9968 | . 9969 | . 9970 | . 9971 | . 9972 | . 9973 | . 9974 |
| 2.8 | . 9974 | . 9975 | . 9976 | . 9977 | . 9977 | . 9978 | . 9979 | . 9979 | . 9980 | . 9981 |
| 2.9 | . 9981 | . 9982 | . 9982 | . 9983 | . 9984 | . 9984 | . 9985 | . 9985 | . 9986 | . 9986 |
| 3.0 | . 9987 | . 9987 | . 9987 | . 9988 | . 9988 | . 9989 | . 9989 | . 9989 | . 9990 | . 9990 |
| 3.1 | . 9990 | . 9991 | . 9991 | . 9991 | . 9992 | . 9992 | . 9992 | . 9992 | . 9993 | . 9993 |
| 3.2 | . 9993 | . 9993 | . 9994 | . 9994 | . 9994 | . 9994 | . 9994 | . 9995 | . 9995 | . 9995 |
| 3.3 | . 9995 | . 9995 | . 9995 | . 9996 | . 9996 | . 9996 | . 9996 | . 9996 | . 9996 | . 9997 |
| 3.4 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9997 | . 9998 |

